Mechanism design and allocation algorithms for energy-network markets with piece-wise linear costs and quadratic externalities

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- Introduction and motivation
- Modeling market and Equilibrium. Discontinuous Games
- Nash and beyond
- Intrinsic market Power
- Efficient regulations and Extended Mechanism Design
- Conclusions

# Introduction and motivation

- Modeling Market
   Equilibrium: Nash
- Intrinsic Market Power
- Efficient regulations and mechanism design
   The benchmark game
  - Comparing Benchmark with Optimal Mechanism

Intrinsic Market Power

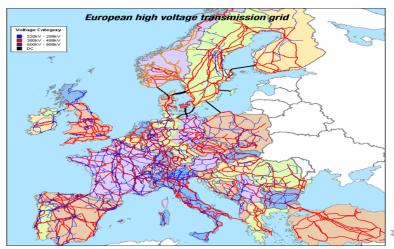


- Most of ISOs have few generation companies: oligopoly
- Transmission networks highly congested in some areas
- Intrinsic market power produced by externalities and information asymmetries

Intrinsic Market Power

Efficient regulations and mechanism design

# **Transmission Europe**



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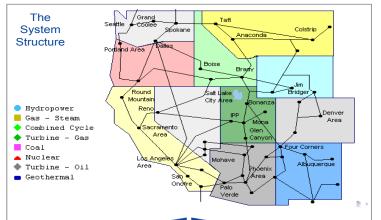
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## **Transmission California**

Electricity System Structure





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## Transmission Brazil: ONS

#### Brazilian Interconected Power System - BIPS



- Multi-owned: 97 agents own assets (≥ 230 kV)
- The Main Transmission Grid is operated and expanded in order to achieve safety of supply and system optimization
- Inter-regional and inter-basin transmission links allow interchange of large blocks of energy between regions, based on the hydrological diversity between river basins
- The current challenge is the interconnection of the projects in the Amazonian Region

#### ONS: F.J. Arteiro de Oliveira

5 ONS Operator Nacional

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#### Introduction and motivation

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Intrinsic Market Power

# A generation short term market: day-ahead mandatory pool

- Today: generators taking into account an estimation of the demand bid *increasing piece-wise linear cost functions or equivalently piece-wise constant "price"*. Even general convex cost functions.
- Tomorrow: the (ISO) using this information and knowing a realization of the demand, minimizes the sum of the costs to satisfy demands at each node considering all the transmission constraints: "dispatch problem".
- Tomorrow: the (ISO) sends back to generators the optimal quantities and "prices" (multipliers associated to supply = demand balance equation at each node)

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# ISO New England adjusts to changing electricity market



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## ISO problem or dispatch DP(c, d)

The (ISO) knows a realization of the demand  $d \in \mathbb{R}^V$ , receives the costs functions bid  $(c_i)_{i \in G}$  and compute:  $(q_i)_{i \in G}$ ,  $(\lambda_i)_{i \in G}$ 

$$\min_{(h,q)} \quad \sum_{i \in G} c_i(q_i). \tag{1}$$

$$\sum_{e \in K_i} \frac{r_e}{2} h_e^2 + d_i \le q_i + \sum_{e \in K_i} h_e sgn(e, i), \quad i \in G$$
(2)

$$q_i \in [0, \bar{q}_i], \quad i \in G, \tag{3}$$

$$0 \le h_e \le \overline{h}_e \tag{4}$$

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We denote  $Q(c, d) \subset \mathbb{R}^G$  the generation component of the optimal solution set associated to each cost vector submitted  $c = (c_i)$  and demand d. We denote  $\Lambda(c, d) \subset \mathbb{R}^G$  the set of multipliers associated to the supply=demand in the ISO problem.

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# Modeling Generators



1 At each node  $i \in G$  we have a generator with payoff

$$u_i(\lambda, q) = \lambda q - \bar{c}_i(q)$$

 $\bar{c}_i$  is the real cost.

The strategic set for each player i denoted S<sub>i</sub>:

 $\{c_i \colon \mathbb{R} \to \mathbb{R}_+ \mid \text{ convex, nondecreasing, bounded subgradients or } \}$  $\partial c_i \subset [0, p^*]$ ,  $p^*$  is a price cap.

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Equilibrium: Nash							
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# Equilibrium

An equilibrium is  $(q, \lambda, m)$  such that q is a selection of  $Q(\cdot, \cdot)$ and  $\lambda$  is a selection of  $\Lambda(\cdot, \cdot)$  and  $m = (m_i)_{i \in G}$  is a mixed-strategy equilibrium of the generator game in which each generator submits costs  $c_i \in S_i$  with a payoff

$$\mathbb{E}u_i(\lambda_i(c,\cdot),q_i(c,\cdot)) = \int_D [\lambda_i(c,d)q_i(c,d) - \bar{c}_i(q_i(c,d))]d\mathbb{P}(d),$$

Neutral or risk averse

#### Remark: this game is played everyday !

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Equilibrium: Nash							
Lite	rature						

- In some cases, for example, using a supply function equilibria approach there are previous works by Anderson, Philpott, or using variational inequality approach by Pang, Ralph, Ferris or also using game theory by Hogan, Smeers, Wilson, Joskow, Tirole, Hobbs, Oren, Borestein, Wolak...
- Limited network representation or strategic behavior or strategy space.
- What is the behavior of this game? How the ISO is interacting with the players?

Outline Introduction and motivation
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Equilibrium: Nash

# Nash equilibrium

Consider a game  $G = (X_i, u_i)^N$  that consists of N players where each player i = 1, ..., N has a strategy set  $X_i$  and a payoff function  $u_i : X \to \mathbb{R}$ , where  $X = \prod_{i \in N} X_i$ .

Nash equilibrium  $(x_i^*)$ 

$$x_i^* \in \operatorname{argmax} \{u_i(x_i, x_{-i}^*) | x_i \in X_i\}$$

Intrinsic Market Power

Equilibrium: Nash

# Nash equilibrium

For the sake of simplicity, we assume that each  $X_i$  is contained in a metric vectorial space:

- If for all *i* the strategy set *X<sub>i</sub>* is a compact set, and *u<sub>i</sub>* is a bounded function, we say that *G* is a *compact game*.
- If for all *i* the set  $X_i$  is convex and for each  $x_{-i} \in X_{-i}$ ,  $u_i(\cdot, x_i)$  is a (concave) quasiconcave function, then we say that *G* is a *convex game* (*quasiconvex game*)

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Equilibrium: Nash

# Nash equilibrium existence

A convex compact game  $G = (X_i, u_i)^N$  satisfying:

- $u_i(\cdot, \cdot)$  is upper semicontinuous
- $u_i(x_i, \cdot)$  is lower semicontinuous for all  $x_i$

has a Nash equilibrium point.

Extensions: generalized games, convergence-stabilty lopsided convergence

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Equilibrium: Nash

## Discontinuos games: tie-breaking rules

Consider the following two-player game: Let the payoff for the i player be given by

$$u_{i}(x_{i}, x_{-i}) = \begin{cases} l_{i}(x_{i}) & \text{if } x_{i} < x_{-i}, \\ \varphi(x_{i}) & \text{if } x_{i} = x_{-i}, \\ m_{i}(x_{-i}) & \text{if } x_{i} > x_{-i}, \end{cases}$$
(5)

where  $x_i \in [0, 1]$ . Assume that for all i and  $x \in [0, 1]$  (a)  $l_i$  and  $m_i$  are continuous functions,  $l_i$  is nondecreasing  $\varphi(x)$  is a convex combination of  $l_i(x)$  and  $m_i(x)$ ; sign  $[l_i(x) - \varphi(x)] = \text{ sign } [\varphi_{-i}(x) - m_{-i}(x)]$ .

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Equilibrium: Nash

# Existence discontinuos games

#### Reny (1999) Econometrica

#### Theorem

A compact quasiconcave game possesses a Nash equilibrium if it is also a better reply secure game.

Bagh and Jofre (2006) Econometrica

#### Theorem

If  $(X_i, u_i)^N$  is weakly reciprocally upper semicontinuous and payoff secure, then it is better reply secure.

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Equilibrium: Nash								

# **Assumptions**

S1. For all  $d \in D$ , there exists  $\delta_d > 0$  such that

$$\Omega(d) \neq \emptyset, \quad \|\hat{d} - d\| \le \delta_d.$$

S2. *D* is compact S3. (1) Either  $\mathbb{P}$  is non atomic; or (2) given two convex sets  $M, N \subset \mathbb{R}^G$ ,  $u(M \times N)$  is convex. S4  $u_i \colon \mathbb{R}^2 \to \mathbb{R}$  is continuous.

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Equilibrium: Nash

# Equilibrium existence

#### Theorem

If each  $S_v$  is a nonempty closed set for the point-wise convergence, then there exists an equilibrium  $(q, \lambda, m)$  for the bid-based generator pool game.

*Example: In real system... increasing piece-wise constant cost functions* 

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Modeling Market
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## Intrinsic Market Power

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Intrinsic Market Power

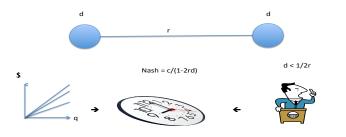
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#### Two-node case

#### Two nodes case

#### Symmetric Nash equilibrium

Profit = multiplier × quantity - cost × quantity



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## the ISO Problem: two-node case

Given that each generator reveals a cost  $c_i$ , the (ISO) solves:

$$\begin{array}{ll} \min_{q,h} & \sum_{i=1}^{2} c_{i}q_{i} \\ s.t. & q_{i}-h_{i}+h_{-i} \geq \frac{r}{2}[h_{1}^{2}+h_{2}^{2}]+d \ \ \text{for} \ \ i=1,2 \\ & q_{i},h_{i} \geq 0 \ \ \text{for} \ \ i=1,2 \end{array}$$

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• Escobar and J. (ET (2010)) equilibrium exists but producers charge a price above marginal cost:

$$Nash = \bar{c}/(1 - 2rd)$$

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# Sensitivity formula

#### Proposition

Let  $c \in \prod_{i \in G} S_i$  and  $c_i - \hat{c}_i$  a Lipschitz function with constant  $\kappa$ . Then,

$$|Q_i(c,d) - Q_i(\hat{c}_i, c_{-i}, d)| \le \kappa \eta,$$

where 
$$\eta = 2 \frac{(1+r_i \bar{h}_i)^2}{\min_{i \in G} r_i c_i^+(0)} \in ]0, +\infty[$$
 and  $c_i^+(0) = \lim_{y \to 0+} \frac{c_i(y) - c_i(0)}{y}.$ 

Why? losses => the second-order growth

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## Market Power formula

#### Proposition

The equilibrium prices  $p_i$  satisfy

$$\mathbb{E}|p_i - \gamma| \ge \frac{\mathbb{E}[Q_i(p_i, p_{-i}, d)]}{\bar{\eta}_i}$$

where  $\bar{\eta}_i = 2 \frac{|K_i|^2 \left(1 + \max\{r_e \overline{h}_e : e \in K_i\}\right)^2}{p_* \min_{e \in K} r_e}$ 

 $\gamma(p_{-i}, d)$  is a measurable selection of  $\partial \bar{c}_i(Q_i(p_i, p_{-i}, d))$ .

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## Market Power formula

#### Proposition

Linear case:  $\bar{c}_i(q) = \bar{c}_i q$ , then

$$p_i - \bar{c}_i \ge \frac{\mathbb{E}[Q_i(p_i, p_{-i}, d)]}{\bar{\eta}}.$$

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- The benchmark game
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Intrinsic Market Power

# The Questions

In an electric network with **transmission costs** and **private information**:

- Does the usual (price equal Lagrange multiplier) regulation mechanism minimize costs for the society?
- If not, what is the mechanism that achieves this objective?
- How does the performance of both systems compare?

Methodology:

- Bayesian Game Theory
- Mechanism Design

Intrinsic Market Power



- A network with demand *d* at each node.
- One producer at each node, with piece-wise linear cost of production c<sub>i</sub> ~ F<sub>i</sub>[c<sub>i</sub>, c<sub>i</sub>]. Common knowledge ! This game is played everyday !
- Transmission costs *rh*<sup>2</sup>, with *h* the amount sent from one node to another.

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## ISO for piece-wise linear cost functions

#### Problem

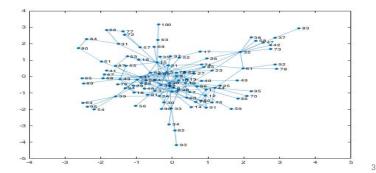
 $\sum_{i=1}^{n} \sum_{j=1}^{n} q_{i,j} c_{i,j}$ minimize (q,h) $i = 1 \ i = 1$  $\sum_{i=1}^{N} q_{i,j} + \sum_{i=1}^{N} h_{i',i} - h_{i,i'} - \frac{h_{i,i'}^2 + h_{i',i}^2}{2} r_{i,i'} \ge d_i \quad (\lambda_i)$ i=1  $i' \in V(i)$  $\forall (i, i') \in E : h_{i,i'} \ge 0 \quad (\gamma_{i,i'})$  $\forall i \in I, j \in J : q_{i,j} \ge 0 \quad (\mu_{i,j})$  $\forall i \in I, j \in J : q_{i,j} \leq \bar{q} \quad (\nu_{i,j}).$ (6)

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## 100 nodes network



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## The ISO Problem: two-node case

Given that each generator reveals a cost  $c_i$ , the ISO solves:

$$\begin{array}{ll} \min_{q,h} & \sum_{i=1}^{2} c_{i}q_{i} \\ s.t. & q_{i}-h_{i}+h_{-i} \geq \frac{r}{2}[h_{1}^{2}+h_{2}^{2}]+d \ \ \text{for} \ \ i=1,2 \\ & q_{i},h_{i} \geq 0 \ \ \text{for} \ \ i=1,2 \end{array}$$

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## The Solution for ISO problem

#### If we define

$$H(x,y) = d + \frac{1}{2r} \left(\frac{x-y}{x+y}\right)^2 - \frac{1}{r} \left(\frac{x-y}{x+y}\right)$$

and

$$\overline{q} = 2\left[\frac{1-\sqrt{1-2dr}}{r}\right]$$

then the solution to this problem can be written as

$$\begin{split} q_i(c_i,c_{-i}) &= \begin{cases} H(c_i,c_{-i}) & \text{if } H(c_i,c_{-i}) \geq 0 \text{ and } H(c_{-i},c_i) \geq 0 \\ \overline{q} & \text{if } H(c_{-i},c_i) < 0 \\ 0 & \text{if } H(c_i,c_{-i}) < 0 \\ \lambda_i(c_i,c_{-i}) \equiv p_i(c_i,c_{-i}) = c_i & \text{if } H(c_i,c_{-i}) \geq 0 \end{cases} \end{split}$$

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#### The benchmark game

### The Bayesian Game: benchmark

### The game:

- 2 players. Strategies  $c_i \in C_i = [\underline{c}_i, \overline{c}_i]$ , i=1,2.
- Payoff  $u_i(c_i, c_{-i}) = (\lambda_i(c_i, c_{-i}) \mathbf{c}_i)q_i(c_i, c_{-i}),$

where  $\mathbf{c}_i$  is the real cost. The Equilibrium:

- A strategy  $b_i : [\underline{c}_i, \overline{c}_i] \longrightarrow \mathbb{R}^+$  (convex at equilibrium!)
- In a Nash equilibrium

$$\bar{b}(c) \in \arg\max_{x} \int_{C_{-i}} [\lambda_i(x, \bar{b}(c_{-i})) - c] q_i(x, \bar{b}(c_{-i})) f_{-i}(c_{-i}) dc_{-i}$$
(7)

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The benchmark game

### **Numerical Approximation**

- For simplicity  $C_i = [1, 2]$ .
- Let  $k \in \{0, ..., n-1\}$ , and  $b(c) = b_k$  for  $c \in [\frac{k}{n}, \frac{k+1}{n}]$ .
- The weight of each interval is given by  $w_k = F(\frac{k+1}{n}) F(\frac{k}{n}).$
- The approximate equilibrium is characterized by:

$$b_k \in \arg \max_x \sum_{l=0}^{n-1} [\lambda_i(x, b_l) - r_k] q_i(x, b_l) w_l \quad \text{for all} \quad k \in \{0, ..., n-1\}$$
(8)

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The benchmark game

## Optimal Mechanism. Principal Agent Model (Myerson)

- A direct revelation mechanism M = (q, h, x) consists of an assignment rule  $(q_1, q_2, h_1, h_2) : C \longrightarrow R^4$  and a payment rule  $x : C \longrightarrow R^2$ .
- The ex-ante expected profit of a generator of type c<sub>i</sub> when participates and declares c'<sub>i</sub> is

$$U_i(c_i, c'_i; (q, h, x)) = E_{c_{-i}}[x_i(c'_i, c_{-i}) - c_i q_i(c'_i, c_{-i})]$$

• A mechanism (q, h, x) is feasible iff:

 $\begin{array}{rcl} U_i(c_i,c_i;(q,h,x)) &\geq & U_i(c_i,c_i';(q,h,x)) & \text{for all } c_i,c_i' \in C_i \\ U_i(c_i,c_i;(q,h,x)) &\geq & 0 & \text{for all } c_i \in C_i \\ q_i(c) - h_i(c) + h_{-i}(c) &\geq & \frac{r}{2}[h_1^2(c) + h_2^2(c)] + d & \text{for all } c \in C \\ q_i(c),h_i(c) &\geq & 0 & \text{for all } c \in C \end{array}$ 

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### The Regulator's Problem

Using the revelation principle, the regulator's problem can be written as:

$$\min \int_{C} \sum_{i=1}^{2} x_{i}(c) f(c) dc$$
(9)  
subject to  $(q, h, x)$  being "feasible"

Existence: Knuster-Tarski fixed point theorem (monotone relations)

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### The Regulator's Problem (II)

### It can be rewritten as

$$\begin{array}{ll} \min & \int_{C} \sum_{i=1}^{2} q_{i}(c) [c_{i} + \frac{F_{i}(c_{i})}{f_{i}(c_{i})}] f(c) dc \\ \text{s.t} & \int_{C_{-i}} q_{i}(c_{i}, c_{-i}) f_{-i}(c_{-i}) dc_{-i} \text{ is non-increasing in } c_{i} \\ & q_{i}(c) - h_{i}(c) + h_{-i}(c) \geq \frac{r}{2} [h_{1}^{2}(c) + h_{2}^{2}(c)] + d \text{ for all } c \in C \\ & q_{i}(c), h_{i}(c) \geq 0 \text{ for all } c \in C \end{array}$$

We denote by  $J_i(c_i) = c_i + \frac{F_i(c_i)}{f_i(c_i)}$  the virtual cost of agent *i*. We assume it is increasing (Monotone likelihood ratio property: true for any log concave distribution)

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### An optimal mechanism is given by

$$\begin{split} \hat{q}_i(c_i,c_{-i}) &= \begin{cases} H(J_i(c_i),J_{-i}(c_{-i})) & \text{if } H(J_i(c_i),J_{-i}(c_{-i})) \geq 0 \\ \overline{q} & \text{if } H(J_{-i}(c_{-i}),J_i(c_i)) < 0 \\ 0 & \text{if } H(J_i(c_i),J_{-i}(c_{-i})) < 0 \end{cases} \\ \hat{x}_i(c_i,c_{-i}) &= c_i \hat{q}_i(c_i,c_{-i}) + \int_{c_i}^{\overline{c}_i} \hat{q}_i(s,c_{-i}) ds \end{split}$$

Such mechanism is dominant strategy incentive compatible.

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Comparing Benchmark with Optimal Mechanism

# Comparing Benchmark with Optimal Mechanism

#### We consider the family of distributions with densities

$$f_a(x) = \begin{cases} a(x-1) + (1 - \frac{a}{4}) & \text{if } x \le 1.5\\ -a(x-1) + (1 + \frac{3a}{4}) & \text{if } x \ge 1.5 \end{cases}$$

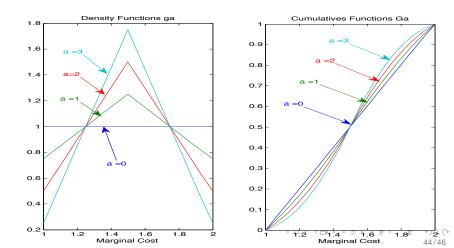
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Comparing Benchmark with Optimal Mechanism

### Asymmetric information

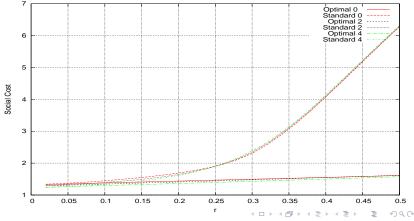


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Comparing Benchmark with Optimal Mechanism

### Social costs for different mechanisms



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Comparing Benchmark with Optimal Mechanism

## **Robustness and Practical Implementation**

• The optimal mechanism is detail free. If the designer is wrong about common beliefs, then the mechanism is still not bad:

$$||X_f - X_{\tilde{f}}|| \le ||x||_1 ||f - \tilde{f}||_{\infty} \le \bar{c}\bar{q}||f - \tilde{f}||_{\infty}$$

- The assignment rule is computationally simple to implement. It requires solving **once** the dispatcher problem, with modified costs.
- However, the payments are computationally difficult

$$c_i \hat{q}_i(c_i, c_{-i}) + \int_{c_i}^{\overline{c}_i} \hat{q}_i(s, c_{-i}) ds$$

#### Comparing Benchmark with Optimal Mechanism

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